

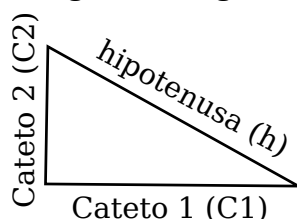
TRIGONOMETRIA

RESOLUCION DE TRIANGULOS

Suma de los ángulos de un triángulo

$$\hat{A} + \hat{B} + \hat{C} = 180$$

Triángulos rectángulos



Teorema de Pitágoras

$$h^2 = c_1^2 + c_2^2$$

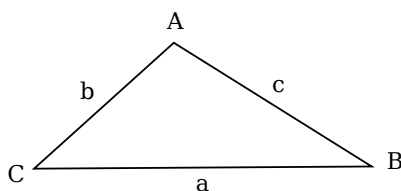
Relaciones trigonométricas

$$\text{Sen } \alpha = \frac{\text{Cateto opuesto}}{\text{hipotenusa}}$$

$$\text{cos } \alpha = \frac{\text{Cateto contiguo}}{\text{hipotenusa}}$$

$$\text{tan } \alpha = \frac{\text{sen } \alpha}{\text{cos } \alpha} = \frac{\text{Cateto opuesto}}{\text{Cateto Contiguo}}$$

Triángulos no rectángulos



Teorema de seno

$$\frac{a}{\text{sen } \hat{A}} = \frac{b}{\text{sen } \hat{B}} = \frac{c}{\text{sen } \hat{C}}$$

Teorema del coseno

$$a^2 = b^2 + c^2 - 2bc \cos \hat{A}$$

$$b^2 = a^2 + c^2 - 2ac \cos \hat{B}$$

$$c^2 = a^2 + b^2 - 2ab \cos \hat{C}$$

FORMULAS TRIGONOMETRICAS

Fórmulas pitagóricas

$$\sin^2(\alpha) + \cos^2(\alpha) = 1$$

$$1 + \text{tag}^2(\alpha) = \frac{1}{\cos^2(\alpha)}$$

Ángulos opuestos

$$\sin(-\alpha) = -\sin(\alpha)$$

$$\cos(-\alpha) = \cos(\alpha)$$

$$\text{tag}(-\alpha) = -\text{tag}(\alpha)$$

Ángulos complementarios

$$\sin\left(\frac{\pi}{2} - \alpha\right) = \cos(\alpha)$$

$$\cos\left(\frac{\pi}{2} - \alpha\right) = \sin(\alpha)$$

$$\text{tag}\left(\frac{\pi}{2} - \alpha\right) = \text{cotag}(\alpha)$$

Ángulos suplementarios

$$\sin(\pi - \alpha) = \sin(\alpha)$$

$$\cos(\pi - \alpha) = -\cos(\alpha)$$

$$\text{tag}(\pi - \alpha) = -\text{tag}(\alpha)$$

Suma/resta de ángulos

$$\sin(\alpha \pm \beta) = \sin(\alpha) \cdot \cos(\beta) \pm \cos(\alpha) \cdot \sin(\beta)$$

$$\cos(\alpha \pm \beta) = \cos(\alpha) \cdot \cos(\beta) \mp \sin(\alpha) \cdot \sin(\beta)$$

$$\text{Tag}(\alpha \pm \beta) = \frac{\text{tag}(\alpha) \pm \text{tag}(\beta)}{1 \mp \text{tag}(\alpha) \cdot \text{tag}(\beta)}$$

Ángulo doble

$$\sin(2\alpha) = 2\sin(\alpha) \cdot \cos(\alpha)$$

$$\cos(2\alpha) = \cos^2(\alpha) - \sin^2(\alpha)$$

$$\text{tag}(2\alpha) = \frac{2 \cdot \text{tag}(\alpha)}{1 - \text{tag}^2(\alpha)}$$

Ángulo mitad

$$\sin\left(\frac{\alpha}{2}\right) = \sqrt{\frac{1 - \cos(\alpha)}{2}}$$

$$\cos\left(\frac{\alpha}{2}\right) = \sqrt{\frac{1 + \cos(\alpha)}{2}}$$

$$\text{tag}\left(\frac{\alpha}{2}\right) = \sqrt{\frac{1 - \cos(\alpha)}{1 + \cos(\alpha)}}$$

Principales valores trigonométricos

| | 0° | 30° | 45° | 60° | 90° | 180° | 270° | 360° |
|-----|----|----------------------|----------------------|----------------------|----------|------|----------|------|
| Sen | 0 | $\frac{1}{2}$ | $\frac{\sqrt{2}}{2}$ | $\frac{\sqrt{3}}{2}$ | 1 | 0 | -1 | 0 |
| Cos | 1 | $\frac{\sqrt{3}}{2}$ | $\frac{\sqrt{2}}{2}$ | $\frac{1}{2}$ | 0 | -1 | 0 | 1 |
| Tag | 0 | $\frac{\sqrt{3}}{3}$ | 1 | $\sqrt{3}$ | ∞ | 0 | ∞ | 0 |